Improving the estimation of $L_{\infty}$

by

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This contribution is the second of a series, addressed to users of the ELEFAN programs, on how to improve their version and use of ELEFAN I and II.

In the first contribution of this series, an outline was given of an approach to improve the estimation of the $K$ parameter of the von Bertalanffy growth equation using ELEFAN I.

Here, four simple approaches for improved estimation of $L_{\infty}$ are presented which rely on slightly modified versions of ELEFAN I and/or II. These approaches are all geared toward counteracting the tendency of ELEFAN I to overestimate $L_{\infty}$.

Approach I: Excluding isolated large fishes from samples analyzed

In ELEFAN I, isolated large fishes (i.e., fishes not part of a contiguous distribution (see Fig 1) have a very strong impact on $L_{\infty}$ estimates i.e.:

1) In the present versions of the ELEFAN system, $L_{\infty}$ cannot be smaller

Fig. 1. Schematic representation of a non-contiguous length-frequency distribution, and definition of its contiguous parts and isolated peaks. Removal of isolated frequencies from original sample lowers the limit for the lowest possible value of $L_{\infty}$ that can be handled by ELEFAN I.

than the upper class limit of the largest class included, plus 1/2 a class interval, and

11) In old versions of ELEFAN I, isolated peaks (such as generated by a single isolated fish) were given a relatively high number of positive "points".

Thus, deleting the fish in the highest length class(es) from the length-frequency sample(s) to be analyzed by ELEFAN I will usually result in lower estimates of $L_{\infty}$. However, this deletion may also result in total mortality being overestimated by ELEFAN II, since old fish will be missing when $Z$ is estimated via catch curve or mean length.

Approach II. Modifying ELEFAN I such as to reduce the impact of isolated large fishes

Two small modifications of ELEFAN I can be implemented which will reduce the impact of large fish on the computation of ESP and hence on the estimation of $L_{\infty}$. They are:

i) Attributing less positive "points" to isolated peaks (i.e., peaks surrounded by zero frequencies) than is done in older version of ELEFAN I, and

ii) Attributing less negative "points" to the highest length classes in a set of samples to be analyzed.

The first of these two modifications refers to the "routine to deemphasize isolated peaks" (see REMs in Pauly et al 1980). The modification suggested is to divide the number of points originally attributed to a length class belonging to isolated peak by $2^n$, where $n$ is the number of zero frequencies within 2 classes (up or down) of length class "1" (the division by $2^n$ should replace the multiplicative factor $(1 - 0.2n)$ used in older versions of ELEFAN I).

The second modification consists of identifying the highest length class in the set of samples to be analyzed ($L_{\text{max}}$), and the class immediately preceding it ($L_{\text{max}-1}$) (these classes may occur in one or several samples of a given length-frequency data set).
Then, if found to be negative, the "point" value for the class corresponding to $L_{\text{max}}$ is set equal to zero, while the "point" value for the class corresponding to $L_{\text{max}}-1$ is multiplied by 0.5 if it also was negative (if the points corresponding to $L_{\text{max}}$ and $L_{\text{max}}-1$ are positive, they should be left as they are). This modification will have the effect of making it unnecessary for the growth curve to "avoid" passing through the classes corresponding to $L_{\text{max}}$ and $L_{\text{max}}-1$ by "aiming" at a higher $L_\infty$ value. (Note with regard to the previous contribution in this series that, while positive point values are counted only once when computing ESP, negative point values are still counted every time their corresponding classes are hit).

**Approach III. Estimating $L_\infty$ Independently of growth data**

Wetherall (see p. 12-14) and Wetherall et al (in press) have developed an extremely ingenious method for estimation of $L_\infty$ from length-frequency data representative of a steady-state population (i.e. the type of data used to construct length-converted catch curves) and which does not require the associated value of $K$ to be known.

Obviously, this method may be incorporated into ELEFAN II, and used to estimate $L_\infty$ from a length-frequency data file entered via ELEFAN 0, based on the routine for summation of samples built into ELEFAN II for construction of length-converted catch curves.

One modification suggested here and which will be incorporated in future versions of ELEFAN II is that instead of plotting the successive mean lengths ($\bar{L}_1$) against their corresponding values of ($L'_1$) one should plot $\bar{L}_1 - L'_1$ on $L'_1$, which results in

$$\bar{L}_1 = a + b L'_1$$

(1)

where

$$L_\infty = a/b$$

(2)

and

$$Z/K = (1 + b)/-b$$

(3)

$\bar{L}_1$ is defined here as the mean length, computed from $L'_1$ upward, in a given length-frequency sample (representative of a steady-state population with constant exponential decay and von Bertalanffy growth). $L'_1$ is the limit of the first length class used in computing a mean length $\bar{L}_1$.

This plot (see Fig. 2) appears easier to interpret visually than the one suggested by Wetherall (this vol., see p. 12-14) and does not lead to an estimate of $L_\infty$ obtained via division by a small difference.

**Approach IV. Allowing $L_\infty$ to be smaller than $L_{\text{max}}$ by modifying ELEFAN I**

The ultimate approach to solving the problem of the overestimation of $L_\infty$ is, obviously, to modify ELEFAN I such that it accommodates values of $L_\infty$ smaller than $L_{\text{max}}$. Versions of ELEFAN I are available for use on Apple II (CP/M) and IBM PC (& compatibles) which incorporate this modification, as well as those discussed under Approaches II and III (Brey and Pauly 1986). Readers are invited to write to this author concerning availability of these programs.

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Of the four approaches presented here to improve estimation of \( L_\infty \), the third is probably the most useful, and the one which will lead, once implemented, to the largest improvements of estimates of \( L_\infty \) from length-frequency data. Nevertheless, readers are encouraged, to also implement the modifications of ELEFAN I suggested in Approach II.

Incorporation of equation (1) as a routine of ELEFAN II should consider the following:
- There should be a graphic display of the values of the points \( (\bar{L}, \bar{L}_1^\frac{1}{2}) \) such as to allow selection of points to be included in the regression equation (as in the case of the length-converted catch curve, which also includes points representing incompletely selected fish that must not be included in the regression), and
- The data points included in the regression should be weighted by the number of fish up to each point.

In the context of the ELEFAN system of programs, the new method for independent estimation of \( L_\infty \) is extremely useful because, after a value of \( L_\infty \) has been estimated, it permits the identification (using ELEFAN I) of the \( K \) value compatible with this (fixed) value of \( L_\infty \). This is a much more rapid procedure which provides values of \( K \) which are much more reliable than when this parameter is estimated together with \( L_\infty \).

The next part of this series shall deal with the effect of incomplete selection and recruitment on estimation of \( L_\infty \) and \( K \) using ELEFAN I, and a simple approach to remove the considerable bias that might occur when uncorrected length-frequency data are analyzed.

References

